

$$= -\frac{4}{3}\pi + \frac{2}{3}\pi^3 \cdot 2 \int_0^{\arcsin(x)} \cos^5 s \, ds \quad (3)$$

$$\cos x = \frac{2\pi}{(8\pi^2)^{3/2}} = 2^{-7/2} \pi^{-2} < 1 < \pi/2$$

$$\int_0^{\arcsin x} \cos^5 s \, ds = \int_0^{\arcsin x} \cos^4 s \cos s \, ds = \left[ \sin s \cos^3 s \right]_0^{\arcsin x} + 3 \int_0^{\arcsin x} \cos^3 s \sin^2 s \, ds$$

per parti

$$\Rightarrow \int_0^{\arcsin x} \cos^5 s \, ds = \frac{1}{4} \left( x (1-x^2)^{3/2} + 3 \int_0^{\arcsin x} \cos^3 s \, ds \right)$$

$$= \frac{x}{4} (1-x^2)^{3/2} + \frac{3}{4} \left[ \frac{s}{2} + \frac{1}{4} \sin(2s) \right]_0^{\arcsin x} = \frac{x}{4} (1-x^2)^{3/2} + \frac{3}{8} \arcsin x + \frac{3}{16} x \sqrt{1-x^2}$$

$$\Rightarrow I = -\frac{4}{3}\pi + \frac{2}{3}\pi^3 x (1-x^2)^{3/2} +$$