

da cui:

$$\begin{aligned}
 \int_{\Sigma} \vec{F} \cdot d\vec{\sigma} &= \iiint_D \nabla \cdot \vec{F} \, dV + \int_{\Sigma_x} (x+x(y-z^2)) \, d\sigma + \int_{\Sigma_y} (2y+y(z^2+x)) \, d\sigma \\
 &+ \int_{\Sigma_z} (3z+z(2z-y-x)) \, d\sigma = \iiint_D \nabla \cdot \vec{F} \, dV \\
 &= \iiint_D 2z \, dV = 2 \int_0^2 z \, dz \int_0^{\sqrt{4-z^2}} \int_0^{\sqrt{4-z^2-y^2}} dx \, dy \, dz \\
 &= 2 \int_0^2 z \, dz \int_0^{\sqrt{4-z^2}} \sqrt{4-z^2-y^2} \, dy \, dz \\
 &= \frac{\pi}{2} \int_0^2 z(4-z^2) \, dz = \frac{\pi}{2} \int_0^4 (4-t^2) \, dt = \\
 &= \frac{\pi}{2} \left[4t - \frac{t^3}{3} \right]_0^4 = \frac{\pi}{2} \left(16 - \frac{64}{3} \right) = 4\pi \left(1 - \frac{4}{3} \right) = \\
 &= -\frac{4}{3}\pi
 \end{aligned}$$