

## Results

The obtained results are shown in terms of *Work Precision Diagrams (WPD)* where, for each code, we plot the execution time versus accuracy. This latter, following the standard of the TestSet for IVP Solvers [1], is measured in terms of *mixed-error significant digits (mescd)*, defined as:

$$\text{mescd} = \max\left\{0, -\log_{10} \max_n \|(y(t_n) - y_n) ./ (1 + |y(t_n)|)\|_{\infty}\right\},$$

where  $y_n \approx y(t_n)$ , this latter the reference solution,  $|y(t_n)|$  is the vector with the absolute values of  $y(t_n)$ , and  $./$  is the component-wise division between vectors.

Some of the parameters used for the code are fixed as follows:

- code `fde12`: `fde12` for PECE and `fde12-10` for  $PE(CE)^{10}$ , respectively;
- code `f1mm2`: used with  $\text{tol} = 10^{-15}$  and  $\text{itmax} = 10^3$ . Moreover, `f1mm2-1`, `f1mm2-2`, `f1mm2-3` will denote the usage of the code with the trapezoidal rule, the Newton-Gregory formula, and the BDF2 method, respectively;
- code `fcoll`: collocation points set at the  $s$  Gauss-Legendre abscissae,  $s = 3, 4, 5$ . Moreover we shall fix the following values of  $r$  for the graded mesh: 1 (if appropriate), 5, and 10. We shall denote `fcoll-s-r` the respective implementations;
- code `tsfcoll`: collocation abscissae set at  $\{1/n, 2/n, \dots, 1\}$ ,  $n = 3, 4, 5$ . Moreover, the parameter  $r$  is fixed as done for `fcoll`, and the respective implementations will be denoted as `tsfcoll-n-r`;
- the codes `fhbvm` and `fhbvm2` have no fixed parameters.

[1 ] <https://archimede.uniba.it/~testset/testsetivpsolvers/>